# AN ACCURATE UPPER ESTIMATE FOR THE TRANSMISSION OF SOLAR RADIATION IN SALT GRADIENT PONDS

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Abstract-The objective of the present work is the estimation of maximum transmission of solar radiation within a body of natural water under the most favorable conditions, with special reference to salt gradient solar ponds.

The study, based on recent data, includes two alternative analytical approaches based on the split of the solar spectrum into the appropriate number of spectral bands and numerical calculation of discrete • values of integrals according to Beer's law. As far as radiation transmission properties of clear water are concerned, it was found that the broadly used absorption law, which is commonly referred to as an upper transmission limit, is derived from original work by Schmidt[23] and deficient data, employed at the time, are responsible for the appreciably lower theoretical maximum transmission then derived. The accurate upper transmission limit derived now also gives comparative higher heat collection efficiency. Comments have been made for the introduction of a water clarity dimensionless factor in terms of the upper transmission limit, describing the economical operation limits for solar pond water.

solar ponds is an important research topic, as better analyses and measurements, to calculate accurately<br>the search the south units leads to get an upper theoretical transmission limit, and to extransmission through the pond water leads to pro-<br>annihilar the inplications to the calculated thermal per-<br>annihilar tis implications to the calculated thermal perportionally more heat being collected at the lower amine its formance. convecting zone. However, even though the stagnant mass of the salt-stratified brine provides very good 2. BACKGROUND THEORY thermal insulation, its fundamentally poor radiation transmission properties are responsible for relatively Solar energy radiation, penetrating the surface of low heat collection efficiencies, a body of natural water, will suffer a decrease in in-

of solar radiation transmission in natural waters for energy by pure water and suspended and dissolved applications in oceanography, as the underwater light matter. greatly affects the life in the oceans and, more re- Although absorbed energy is transformed mainly cently, for water pollution control in natural lakes and to heat and, to a small extent, to chemical energy, reservoirs. The need for a typical radiation transmis- scattering, which is caused by reflection and diffracsion model for solar pond research applications has tion at small particles and colloidal solutions, is remotivated various recent investigators to reassess the sponsible for changing the direction of light and can previous work and to develop simple methods to de- be noticed by an observer outside the path of direct scribe solar energy absorption within the pond waters, light rays as Tyndall light.

function that was suggested by Rabl and Nielsen<sup>[1]</sup>,  $s/\lambda^n$ , where s is the volume concentration of scatwas based on earlier calculations on distilled water terers. When size of scattering particles is small comdata and was extensively employed in solar pond per-<br>pared to the wavelength  $\lambda$ , then  $n = 4$  (Rayleigh scatformance predictions. It has become known as an up- tering), otherwise  $n < 4$ . per transmission limit to solar radiation, as the pond The scattering of light in optically pure water is waters never would be expected as clear as distilled due to the Brownian motion of water molecules, which water, causes very small density fluctuations and therefore

merits[2] that appeared sporadically in the literature irregular variations of light refraction in spaces of and recent calculations--also based on distilled water molecular size[3]. Each of the above phenomena, data-showed appreciably higher transmission con-<br>which independently contributes to the decrease of ditions. This is found to be in open conflict with the radiation intensity, is characterized by an extinction widely employed four exponential term transmission coefficient that is strongly wavelength dependent, and function. The overall extinction of radiation phenomenon is de-

1. INTRODUCTION The aim of this work is to give reasonable expla-The transmission of solar radiation in salt gradient nations to the discrepancies found between previous analyses and measurements, to calculate accurately

The earlier investigations involved the estimation tensity as a result of absorption and scattering of

The derived four exponential term transmission The intensity of scattered light is proportional to

Therefore, very high transmission measure- optical inhomogeneities in the water, which lead to scribed by the wavelength-dependent extinction coefficient:

$$
E(\lambda) = k(\lambda) + \varepsilon(\lambda) + k_w(\lambda) + \varepsilon_w(\lambda)
$$

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where k and  $k_{w}$  denote absorption by pure water and <br>by suspended and dissolved matter, respectively and  $\qquad \qquad$  li by suspended and dissolved matter, respectively, and  $\varepsilon$ ,  $\varepsilon$ <sub>*w*</sub> denote scattering by pure water and by suspended and dissolved matter, respectively.

ficient  $E$  for the total radiated energy, although it numerical radiated energy, although it should be kept in mind that the solar spectrum penetrating the water body undergoes a dramatic change in spectral composition.  $B(\lambda, x) = B(\lambda, 0) \cdot \exp[-\int E(\lambda, x) \cdot dx]$ 

Mathematically, radiation extinction is described at a certain wavelength  $\lambda$  by Beer's law

$$
B(\lambda, x) = B(\lambda, 0) \cdot \exp[-E(\lambda) \cdot x]
$$

where  $B(\lambda,0)$  is the energy in the solar spectrum at the wavelength  $\lambda$  at  $x = 0$ , (just below the free liquid surface), when  $x$  is the optical depth or the depth in the pond with zero angle of incidence (sun over-<br>head).  $B(\lambda, x)$  is the transmitted energy at depth x and<br> $E(\lambda)$  is the autientian coefficient that isolates heat.  $E(\lambda)$  is the extinction coefficient that includes both phenomena, absorption, and scattering at wavelength Distinct values of both integrals (1) and (2) give  $\lambda$ . Then the total energy of the solar spectrum at the exact values of the transmitted solar radiation at X. Then the total energy of the solar spectrum at the the exact values of the transmitted solar radiation at depth x is given by

$$
B(x) = \int_0^{\infty} B(\lambda, x) \cdot d\lambda
$$
  
= 
$$
\int_0^{\infty} B(\lambda, 0) \cdot \exp[-E(\lambda) \cdot x] \cdot d\lambda
$$

happens in solar pond research, ficient in each band.

$$
B(x) = \int_{\lambda_{\min}}^{\lambda_{\max}} B(\lambda, 0) \cdot \exp[-E(\lambda) \cdot x] \cdot d\lambda \qquad (1)
$$
  

$$
B(x) = \sum_{i=1}^{N} \vec{B}_i \cdot e^{-\vec{E}_i \cdot x}
$$

It is well known that, although the existence of dissolved salts in small concentrations in pure water where does not appreciably affect transmission of radiation, the highly concentrated brines, especially near the bottom of salt gradient solar ponds where the solution , is near saturation, seems to affect radiation transmission considerably.

Previously reported work from Usmanov et al.<sup>[4]</sup> and Lund and Keinonen[5] have shown that function  $E$  is also concentration dependent and, consequently,  $\qquad$  If the total energy content of solar spectrum is depth dependent. It must be noted here though, that Usmanov's extinction data for pure water were found to be appreciably higher than those in the literature  $\vec{B} = \begin{bmatrix} B(\lambda) \cdot d\lambda \\ d\lambda \end{bmatrix}$ at the range between 0.36 and 0.6  $\mu$ .

The extinction of monochromatic radiation in a water layer dx at a depth x from the surface of a solar per unit transmission may be defined as the ratio pond, in which the salt concentration varies linearly with zero salinity concentration at the top, is

$$
dB(\lambda, x) = -E(\lambda, x) \cdot B(\lambda, x) \cdot dx
$$

$$
R(\lambda_{\alpha},x) = -\int_0^x E(\lambda_{\alpha},x) \cdot dx + C
$$

It is possible to define the average extinction coef-<br>It is possible to define the average extinction coef-<br> $\frac{1}{2}$  numerical constant is derived and the expression

$$
B(\lambda_{\alpha},x) = B(\lambda,0) \cdot \exp \bigg[ - \int_0^x E(\lambda_{\alpha},x) \cdot dx \bigg]
$$

The total energy of the spectrum of interest between  $\lambda_{\min}$  and  $\lambda_{\max}$  at depth x is given by

$$
B(x) = \int_{\lambda_{\min}}^{\lambda_{\max}} B(\lambda, 0)
$$
  
 
$$
\cdot \exp\left[-\int_{0}^{x} E(\lambda, x) \cdot dx\right] \cdot d\lambda
$$
 (2)

a given depth x. The functions  $B(\lambda,0)$ ,  $E(\lambda)$ , and  $E(\lambda,x)$ are given graphically or in tabular data form and the integrals can be computed numerically.

To avoid numerical methods, a less complicated, although less accurate approach is offered for the calculation of transmission at a given depth, as a contribution of energy transmission from various portions of the solar spectrum, which is divided into a and if the solar spectral irradiance is considered over number of wavelength bands  $\lambda_1, \lambda_2, \lambda_3, \ldots, \lambda_N, \lambda_{N+1}$ , a definite wavelength range of interest, as is usually according to the mean value of the extinction coef-

Then,

$$
B(x) = \sum_{i=1}^N \vec{B}_i \cdot e^{-\vec{E}_i \cdot x}
$$

$$
\bar{B}_i = \frac{\int_{\lambda_i}^{\lambda_{i-1}} B(\lambda) \cdot d\lambda}{\int_{\lambda_i}^{\lambda_{i-1}} d\lambda} \quad \text{and} \quad \bar{E}_i = \frac{\int_{\lambda_i}^{\lambda_{i-1}} E(\lambda) \cdot d\lambda}{\int_{\lambda_i}^{\lambda_{i+1}} d\lambda}
$$

$$
\bar{B} = \int_{\lambda_i}^{\lambda_{i+1}} B(\lambda) \cdot d\lambda
$$

$$
TR(x) = \frac{B(x)}{\bar{B}}
$$

Obviously, a calculation with a larger number of bands and integrating we have, and integrating we have,  $gives more accurate results.$ 

data are involved with the calculation of the energy filtered clear oceanic water.

ably different from blackbody radiation at the same Petty (1951)[17], and others covering a broad band temperature, due mainly to selective absorption of of wavelengths. It has been proved[16] that the opspectrum by various atmospheric gases. Although the tical properties of doubly distilled and pure water are direct beam radiation spectrum on a horizontal sur- practically the same and the presence of salt in face diminishes rapidly with increasing air mass ac- small concentrations does not affect transmission of cording to Lambert's law, and shifts its energy con- radiation. tent toward longer wavelengths (the most favorable Dietrich[18] has compared and summarized the case is  $AM = 1$  with the sun nearly overhead), the results of investigations, which were performed for diffuse spectrum adds considerable energy in pure water until the late 1930s and presented an exthe UV region and blue. It is generally believed that tinction curve covering the wavelength range bethe diffuse spectrum due to Rayleigh scattering is tween 0.186 to 2.65  $\mu$ , which appears repeatedly in shifted toward shorter wavelengths with peaks near the more recent oceanographical literature[3.19]. 0.33  $\mu$  and 0.41  $\mu$  and there is good agreement be-<br>The results of several more recent investigations

derivation of radiation transmission data and intro- good agreement between older and more recent in-

He assumed this component as isotropic and he cal- differences between various investigators do not greatly culated its transmission by splitting the blackbody affect the shape of the extinction curve. spectrum at sky color temperature corresponding to The most widely known mathematical expression various weather types, on transmission of solar radiation in the literature is

nation of different stochastic variations in the spectral expression, which was approximated by the handy composition of the diffuse radiation spectrum, related algebraic relationship to different weather types and clouds, attention is concentrated on transmission of direct radiation. The fact that diffuse radiation is usually a small portion of the total incident solar energy and is characterized in the range of 10 m  $\ge x \ge 0.01$  m by Bryant and by relatively higher reflection losses at the air-water Colbeck[22]. Although not very accurate for the purinterface, neglecting diffuse radiation with its shorter pose, as it is based on distilled water data, this wavelength content leads to more pessimistic esti-<br>
expression gives an upper theoretical transmission limit

more recently from various researchers on the solar transmission at certain depth, as a contribution of raconstant, spectral distribution of solar radiation, and diation transmission of each one of the four individon the absorption effects of the atmosphere[7-9]. Due ual portions of solar spectrum from 0.2 to 0.6  $\mu$ , 0.6 to the fact that earlier investigations were based on to 0.75  $\mu$ , 0.75 to 0.9  $\mu$ , and 0.9 to 1.2  $\mu$ . extrapolation from ground-based observations, recent According to Rabl and Nielsen, its derivation was observations, made from satellites, prove to be more based on oceanographical data by Defant[19] which accurate, and Thekaekara proposed a standard solar are due to earlier calculations on solar energy despectrum at  $AM = 0$  and reported extensive data on position at various depths in the body of natural waters solar spectral irradiance at sea level and various air by Schmidt[23]. masses[10,11] from which the  $AM = 1$  solar spec-<br>Calculation of Schmidt's tables and diagrams, trum in tabular form was depicted, which can be found in[23], describing the energy

tied out since the late nineteenth century in experi- based on spectral extinction measurements by As-

3. AVAILABLE DATA AND PREVIOUSLY REPORTED mental investigation of spectral extinction coeffi-WORK cients, mainly for doubly distilled water, pure water. and seawater of various origins. In the literature, the Since extinction data and solar spectral irradiance term "pure water" usually means extremely carefully

that is transmitted through the body of natural waters, More and more careful measurements have been a brief discussion is devoted to both of these, which made by Hufner and Albrecht (1891)[ 12], Aschkiwere derived from spectral measurements. The nass (1895)[13], Collins (1925)[14], Sawyer The solar spectrum at sea level appears appreci- (1931)[15], Clarke and James (1939)[16], Curcio and

tween results from theoretical models and field have been reviewed by Hale and Querry[20] and Smith measurements. The and Baker[21], and the derived data from these in-Since incident radiation is composed of direct and vestigations scatter slightly around the extinction curve, diffuse components with vastly different spectral mainly because it is extremely difficult to obtain a composition, these must be treated separately for the standard quality of "optically pure" water. There is duction into computer simulation calculations. The vestigations, especially at wavelengths longer than Hull[6] suggested a simple means of approximat-  $0.5 \mu$ . At shorter wavelengths, reported data by Hale ing the transmission of diffuse radiation in solar ponds, and Querry[20] appear higher. Even so, the small

However, due to the complexity of the combi- the Rabl and Nielsen  $(R-N)[1]$  four exponential term

$$
h(x) = 0.36 - 0.08 \cdot \ln x
$$

mation of transmission of solar radiation.  $\qquad \qquad$  on which numerous solar pond performance predic-Extensive work has been carried out earlier and tions were based. This expression gives the per unit

On the other hand, extensive work has been car- transmission at various depths in a water body, were

chkinass[13] and a solar spectrum at the sea level, 46% higher and greatly affects thermal performance which is due to Langley<sup>[24]</sup> and appears appreciably calculations. different from solar spectral irradiance diagrams ac- The derived amplitudes from Langley's spectrum cording to more recent measurements at sea level and were found to be very close to those of the  $R-N$ <br>AM = 1.

 $AM = 1$  spectrum into a large number of wavelength ergy spectrum was not used. bands and derived a 40-exponential term, 80-param- Aiming at a more logical division of the spectrum eter extinction function. He obtained appreciably in bands according to the energy content, and the corhigher transmission than the values imposed by the responding mean value of extinction coefficient in each previously calculated upper transmission limit and his band, the spectrum was divided into 19 wavelength thermal calculations showed 15 to  $20^{\circ}$ C higher tem- bands. The higher the energy content and the smaller peratures, starting from identical initial conditions, extinction coefficient, the narrower the band.

40-term absorption function and recent absorption data Hull[26] and, which, according to recommendations it comes from greater accuracy of 40 terms. Fig. 1.

R-N function was derived from a simple exponential lar spectrum ( $\alpha = 0.66$ ,  $\beta = 0.085$ ) have been adapted fitting of Defant's data, it is not quite clear from [1] from Thekaekara[11] and is shown by curve 2 in Fig. whether it was derived by calculation using extinc- 1, in which the 19 bands are also shown. The sotion coefficient data applied to the spectrum of in- computed transmission function has the form terest or by simple fitting of Schmidt's data. If it was calculated, it is not known why the divisions were so chosen, as the most of the radiated energy lies within the 0.2 to 0.6- $\mu$  range, since at 0.5  $\mu$  there is a very sensitive transmittance window with significant vari-<br>Constants  $\mu_i$  and  $n_i$ , which are given in columns

energy in Langley's solar spectrum, which was used starting with the  $AM = 1$  solar spectrum as depicted by Schmidt, is shifted toward longer wavelengths, so from Thekaekara[11] and with spectral extinction that the band 0.2 to 0.6  $\mu$  contains appreciably less coefficients as depicted from [27]. In column 4 of energy than is now found. Table 2, the corresponding amplitudes for each of the

the amplitudes of exponential terms were calculated literature for distilled water[21,28], apart from the using the blackbody spectrum at the temperature of work by Usmanov et al.[4] and Lund and Keino-5762 K, a recent AM = 1 solar spectrum at sea level, nen[5], which is not suitable for NaCl salt-water soand Langley's spectrum. The mean extinction coef- lutions, there are very few references to detailed exficients over each band are identical and the results perimental results on extinction measurements in salt are shown in Table 1. As can be seen, the derived solutions of various concentrations in distilled water. amplitudes for blackbody and  $AM = 1$  spectrum show Apparently, there is much need for further work tomuch the same deviation from the R-N function and ward the accurate experimental determination of deare appreciably different from the function widely tailed spectral extinction characteristics of the comused, especially in the amplitude of the most deeply monly employed salts in a range of different penetrating first-term component, which is about concentrations.

 $A = 1$ .<br>Using recent extinction data, Hull(6) divided the that in its initial derivation the appropriate solar enthat in its initial derivation the appropriate solar en-

Even though transmission comparisons between Extinction data are identical to those employed by from clear lake water have shown good agreement of Jerlov[27] have been adapted from measurements according to Hull, there is no explanation of the dif- made by Clarke and James[16] and Curcio and ference in transmission between the 40- and 4-term Petty[17] in the regions between 0.325 to 0.8  $\mu$  and Rabl-Nielsen function, except for the implication that  $0.8$  to 1.3  $\mu$ , respectively, and shown by curve 1 in

A part from an indication in [25] that the 4-term Solar spectral irradiance data for the AM = 1 so-

$$
h(x) = \sum_{i=1}^{19} \mu_i \cdot \exp(-n_i \cdot x)
$$

ations of the extinction coefficient. 3 and 5 of Table 2, were calculated according to the One plausible explanation is that the total radiated presented simplified method in background theory, 19 bands are given comparatively, according to data from Thekaekara[10] for  $AM = 0$ .

4. THE PRESENT WORK To the author's knowledge, although spectral ex-Using the same four divisions of the solar spectrum, tinction coefficient data are readily available in the

Table 1. Exponential term amplitudes, as calculated for various solar energy spectral distributions

Amplitudes	First term	Second term	Third term	Fourth term	Fifth term
Wavelength band	$0.2 - 0.6$	$0.6 - 0.75$	$0.75 - 0.9$	$0.9 - 1.2$	$1.2 - 3$
Four-exponent term R-N function	0.237	0.193	0.167	0.179	0.224
According to recent $AM = 1$					
spectrum	0.346	0.203	0.128	0.153	0.167
Blackbody spectrum at 5762 K	0.391	0.143	0.119	0.129	0.215
Schmidt's spectrum	0.229	0.196	0.150	0.177	0.246



Fig. 1. Division of the AM = 1 solar spectrum at sea level (curve 2), in 19 wavelength bands. Curve 1 shows the shape of the extinction curve according to spectral measurements of extinction coefficient in distilled water.

calculation of integral (2) can give reliable results. Fig. 3 in which curve 1 represents the derived 19 Instead, calculation of (1) is possible from solar spec- exponential term transmission function, curve 2 reptral irradiance and extinction data in tabular form. resents the R-N transmission function, curve 3 the Integrals were calculated numerically by a digital transmission function (which was derived by calcucomputer using the Simpson and Gill-Miller meth-<br>lation of the integral (1)), and curve 4 represents the ods. The results from both methods were almost the almost identical to (3) 40 exponential term Hull's same with differences less than 0.1%. transmission function.

For the purpose of integration, it was found that Curves 5 and 6 represent measurements for clear bands, as can be seen in Fig. 2. exponential term R-N transmission.

Accordingly, it seems improbable that numerical The results of the above calculations are shown in

the division of the spectrum of interest into 100 equally open sea water (Sargasso Sea) as depicted from [29] spaced bands gives good accuracy, whereas accept- and from Castle Lake as depicted from [30], respecable accuracy could be obtained with only 30 or 40 tively. Note that both indicate higher than the four

(1)	(2)	(3) Amplitudes	(5)	
$\boldsymbol{N}$	Wavelength band $(\mu)$	Thekaekara at $AM = 1[11]$	Thekaekara at $AM = 0110$	Extinction coefficient $(m^{-1})[27]$
	$0.200 - 0.400$	0.0466	0.0910	.058
2	$0.400 - 0.425$	0.0290	0.0346	.039
3	$0.425 - 0.450$	0.0345	0.0366	.025
4	$0.450 - 0.475$	0.0408	0.0399	.018
5	$0.475 - 0.500$	0.0413	0.0383	.026
6	$0.500 - 0.525$	0.0400	0.0355	.038
7	$0.525 - 0.550$	0.0390	0.0359	.055
8	$0.550 - 0.575$	0.0375	0.0350	.081
9	$0.575 - 0.600$	0.0375	0.0337	.137
10	$0.600 - 0.625$	0.0367	0.0324	.205
11	$0.625 - 0.650$	0.0360	0.0306	.255
12	$0.650 - 0.675$	0.0350	0.0289	.324
13	$0.675 - 0.700$	0.0327	0.0271	.425
14	$0.700 - 0.750$	0.0629	0.0494	1.33
15	0.750-0.800	0.0548	0.0439	2.2
16	$0.800 - 0.850$	0.0476	0.0390	2.9
17	0.850-0.900	0.0263	0.0346	5.17
18	$0.900 - 1.200$	0.1530	0.1495	42.5
19	1.200–3.000	0.1676	0.1832	1800.0

Table 2. Calculated amplitudes and extinction coefficients for the 19-term transmission function



in the calculated transmission, as it was found for various

untreated pond water from the Miamisburg solar transmission. pond[31] and curve 8 represents data reported by Ta- The derived function may be fitted by polynobor and Matz[2] for the Sdom solar pond. It is re- mials with high accuracy such as the one of fourth markable to note here the high water transparency degree,

near the top surface, which significantly decreases, possibly due to settling of dirt near the bottom of this

The 19-term transmission function gives comparable transmission (difference less than  $2\%$ ) with curve 3, which was derived from calculation of the integral  $\overline{0.5M}$  <sup>o</sup> *o i* which usually correspond to the upper mixing zone  $\frac{1.0 \text{ M}}{2.0 \text{ M}}$  thickness with no effect in the calculation of thermal performance, this difference becomes higher (typicalculation of the integral (1) the I.R. part of the  $\frac{5.0 \text{ M}}{\text{spectrum at longer wavelengths than 1.3 is excluded.}}$ 

It can be seen also that the derived results show about 0.1 better transmission at almost any practical  $20.0 M$   $\bullet$  depth from the R–N function and are identical to Hull's function.

In the same figure, curve 9 represents the transmission function as calculated from numerical inter-*NUMBER OF STEPS* coefficient data and Langley's spectrum, whereas Fig. 2. The effect of the number of the equally spaced bands calculation starting from  $AM = 1$  and the familiar in the calculated transmission as it was found for various division of the spectrum into four wavelength bands depths, in the numerical calculation of intergral (1) (Simp- gives transmission data closely lying to curve (3). This son's method). very probably suggests that while the use of the proper, most favorable  $AM = 1$  spectrum greatly improves the accuracy of calculations, being responsible for the Curves 7 and 8 represent data from actual solar appreciable increase in transmission, the use of coarser ponds. Curve 7 represents typical measurements for or four-band division slightly affects radiation



Fig. 3. Comparison between measurements, previous analyses, and derived results. Curve (l) and (3) show the almost identical results that were derived from the 19 exponential term and numerical intergration and (2) the 4 exponential term R-N function. Also shown are (5), (6), (7), and (8) data from measurements. Curve (9) was derived by numerical intergration starting with spectral extinction data from [27] and Langley's spectrum. Curve (4) represent data derived by Hull[6].

$$
h(x) = 0.67031 - 0.35170 \cdot x + 0.19785
$$
  

$$
\cdot x^2 - 0.05567 \cdot x^3 + 0.00580 \cdot x^4
$$

simple algebraic relationship **per radiation transmission limit for the direct beam** 

$$
h(x) = 0.46 - 0.0953 \cdot \ln x
$$

$$
5.5 \text{ m} \geq x \geq 0.2 \text{ m}
$$

data in a logarithmic graph. The lutely free of organic substances, debris, or algae,

calculated thermal performance, the R-N transmis- carefully filtered oceanic water, but it demonstrates sion function was replaced in our salt gradient solar the improvement in transmission and efficiency that nondel by the derived polynomial an-<br>nond numerical model by the derived polynomial an-<br>may be achieved with a good pond numerical model by the derived polynomial ap-<br>proximation. Typical results are shown in Fig. 4 for ment. The improvement on calculated transmission proximation. Typical results are shown in Fig. 4 for a pond operating in a midlatitude country with astor- now found is due mainly to the selection of the more age zone of 0.8 m, upper mixing zone of 0.1 m, un-<br>derground water flow of 10° C, at 6 m under the bot-<br>mathematical accuracy offered by the employed calderground water flow of  $10^{\circ}$  C, at 6 m under the bottom of the pond with bottom absorptivity  $\alpha_b = 0.85$ , culations.<br>for a gradient zone thicknesses of 0.5, 1.0, and 1.5 There are also important implications in the calfor a gradient zone thicknesses of  $0.5$ ,  $1.0$ , and  $1.5$ m deep. culated thermal performance of salt gradient solar

appreciably improved for the three nonconvecting zone thicknesses over a wide range of operating ficiencies, appreciably higher than those calculated temperatures. The contraction of the state of the state of the state of the four-term transmission function.



Fig. 4. Comparative steady-state, thermal performance results, according to derived and 4 exponential term R-N function for three gradient zone thicknesses. Daily average *ical Oceanography.* Prentice Hall, Englewood Cliffs, (yearly) solar insolation level  $\hat{I} = 180.9 \text{ W/M}^2$ , daily av- N.J. (1966). **erage temperature**  $\hat{T}_A = 18.1^\circ$  **C (38°N Lat., Athens, Greece). 4. Y. Usmanov, V. Eliseev and G. U. Umarov, On the** 

## 5. CONCLUSIONS

It has been found that the R-N four exponential and can be approximated with good accuracy by the term transmission function does not represent the upas it is based on earlier performed calculation. By numerical intergration calculations and by division of the solar spectrum in 19 nonequally spaced bands, it in the useful range of depths was found that an upper theoretical transmission limit for the direct beam could be set if the pond water could be kept as clear as distilled water. This does not necessarily mean that waters of operational ponds which was found by fitting a straight line on derived open to the environment may be kept easily, abso-In order to be able to estimate the effects on the which are responsible for clarity degradation, like

As can be seen, heat collection efficiency is ponds. Introduction of the derived function in ther-<br>recisibly improved for the three nonconvecting mal performance models leads to heat extraction ef-

It is also concluded that for a rough estimation of thermal performance it would be sensible to introduce a water quality dimensionless factor, in terms FOUR EXPONENT. of the upper standard distilled water transmission limit *TERMR-NFUNCTION* for the direct radiation. This factor, describing the  $\,DERIVED \,UPPER$  | practical water transmission limits within which the  $T RANSM. LIMIT$   $\qquad \qquad$  pond could be operated economically, could be set  $\left( \frac{\text{TRANSM. LIM1}}{\text{CURVE 3, FIG. 3}} \right)$  for practically very pure pond water, at such value  $(0.7-0.75)$ , as to give transmittances near the R-N transmission function[32]. Even though distilled-water data have been used in these calculations, some indications in the literature of measurements in clear  $\overline{I}$  = 180.9 W/M<sup>2</sup>  $\left\{\begin{array}{c} x \leq x \\ y \leq x \end{array}\right\}$  natural water (Crater Lake, USA)[33], appear even more favorable. The phenomenon may be possibly  $\overline{T}_{A}=18.1 \degree C$  x  $\left(\frac{1}{2}\right)^{1/2}$  \extributed to the presence of an appreciable diffuse **BOTTOM ABSORPT.**  $\sum_{n=1}^{\infty}$   $\sum_{n=1}^{\infty}$  component that is penetrating the natural water body

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